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# OBSERVING THE INTERACTION OF PMD WITH GENERATION OF NLI IN UNCOMPENSATED AMPLIFIED OPTICAL LINKS

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- Is **NLI generation** the fiber propagation limiting impairment also for **very-large band transmission beyond the C-band**?
- What is the **proper wave equation** to be considered as governing propagation of dual-polarization carrier-less modulation formats relying on coherent & equalized receivers?

# THE MANAKOV EQUATION

- Propagation of PM-xQAM in the fiber is typically analyzed solving the **Manakov Equation (ME)**
- **ME** is the **polarization-averaged** fiber wave equation
- The ME was originally **developed to study solitons**

## On the theory of two-dimensional stationary self-focusing of electromagnetic waves

S. V. Manakov

*Institute of Nuclear Physics, Siberian Division, USSR Academy of Sciences*

(Submitted March 2, 1973)

*Zh. Eksp. Teor. Fiz.* 65, 505–516 (August 1973)

**Sov. Phys.-JETP, Vol. 38, No. 2, February 1974**

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IEEE JOURNAL OF QUANTUM ELECTRONICS, VOL. 15, NO. 12, DECEMBER 1988

## Pulse Propagation in an Elliptically Birefringent Kerr Medium

CURTIS R. MENYUK, SENIOR MEMBER, IEEE

28

JOURNAL OF LIGHTWAVE TECHNOLOGY, VOL. 10, NO. 1, JANUARY 1992

## Polarization Multiplexing with Solitons

Stephen G. Evangelides Jr., *Member, IEEE*, Linn F. Mollenauer, *Member, IEEE*, James P. Gordon, *Senior Member, IEEE*, and Neal S. Bergano, *Senior Member, IEEE*

- **ME+PMD** : the Manakov-PMD equation (MPE)
- **ME and MPE hold only over narrow bandwidths**

JOURNAL OF LIGHTWAVE TECHNOLOGY, VOL. 15, NO. 9, SEPTEMBER 1997

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## Application of the Manakov-PMD Equation to Studies of Signal Propagation in Optical Fibers with Randomly Varying Birefringence

Dietrich Marcuse, *Fellow, IEEE*, C. R. Menyuk, *Senior Member, IEEE*, and P. K. A. Wai, *Senior Member, IEEE*

# ME AND MPE: BANDWIDTH ISSUES

- The fiber is affected by **random birefringence inducing PMD**
- ME and MPE are limited by the **fiber coherence bandwidth:**

$$B_c \cong \sqrt{3 / (4\pi^2 \cdot PMD^2 \cdot L_{eff})}^*$$

- $B_c \cong 500$  GHz in modern fibers
- If the exploited B exceeds  $B_c$ 
  - **Coupled NLSE** including **random birefringence** as fiber wave equation
  - **Monte Carlo** analyses to verify the **PMD effect**

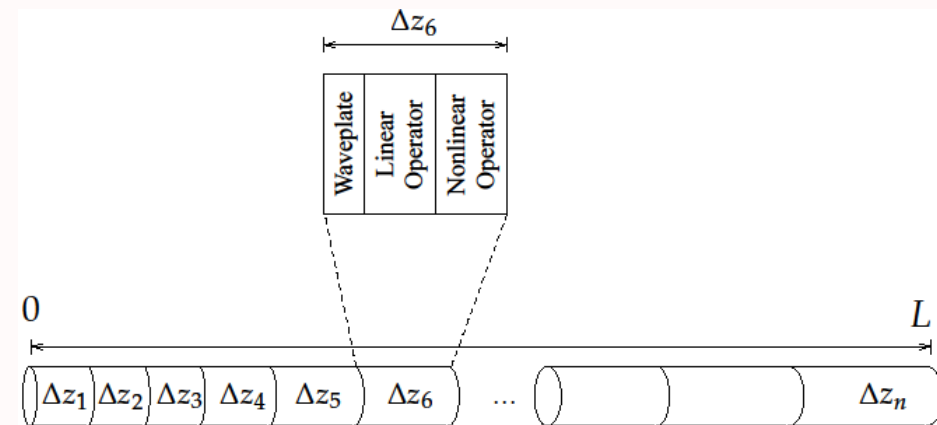
# NONLINEAR INTERFERENCE (NLI)

- **State-of-the art** is polarization-division-multiplexed multilevel modulation formats with **DSP coherent receivers** propagating on **uncompensated links**
- Propagation **impairments** are dominated by the **NLI accumulation**
- After the Rx equalizer and CPE, **NLI is well approximated by four uncorrelated Gaussian random processes**: in-phase and quadrature on two orthogonal polarization states
- **Several models for the NLI** estimation have been developed starting from the ME, so **they in principle hold only over  $B_c$**

- **NLI** generation has been **observed\*** up to **7 THz** of bandwidth occupation for **ASE noise channels**
  - **Good agreement with models** predicting **log-scaling** of **NLI with** the transmission **bandwidth**
  - Indeed, it was predictable, since **ME holds for** any bandwidth in case of propagation of **depolarized Gaussian noise**
- What happens to **NLI when loading spectrum with modulated channels?**
- So, on **which wave equation** we have to rely on?

- **Required investigations**
  - **Modulated channels**
  - **Monte Carlo** analyses varying **PMD** realizations
  - **No recirculating loop**
- Experiments are really **challenging**
- **Split-step simulations** can be feasible **using parallel computing on multicore CPUs and exploiting GPUs**

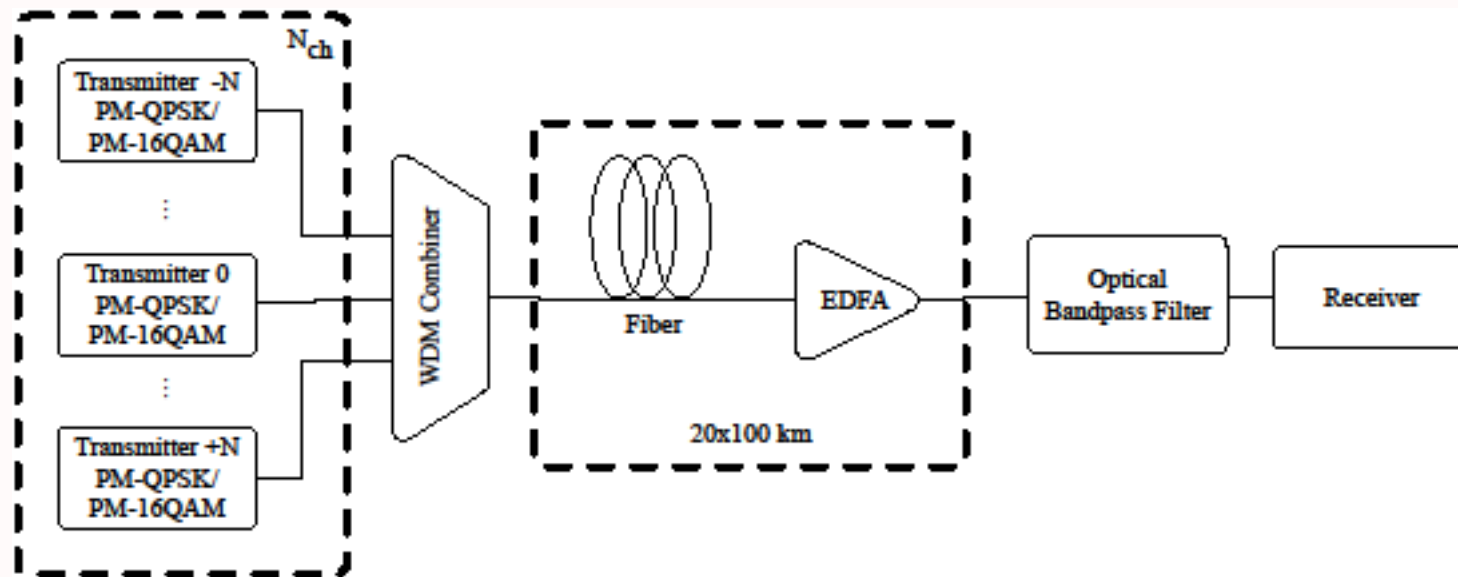
- **Split-step Fourier method** for
  - **Coupled nonlinear Schrödinger** equation jointly solved with
  - **Waveplate** model to emulating random birefringence and induced PMD
  - Machine-tailored Matlab implementation
- **Step size** is the **shortest** between **max NL phase-shift** and **waveplate step**
- Parallel computing and GPU





# THE SIMULATIVE ANALYSIS

- PM-QPSK or PM-16QAM channels at **32 Gbaud**
- $\Delta f = 50 \text{ GHz}$  and  $N_{\text{ch}}$  **up to 41 ch**
- **Link:** 20x100 km of SSMF with EDFA



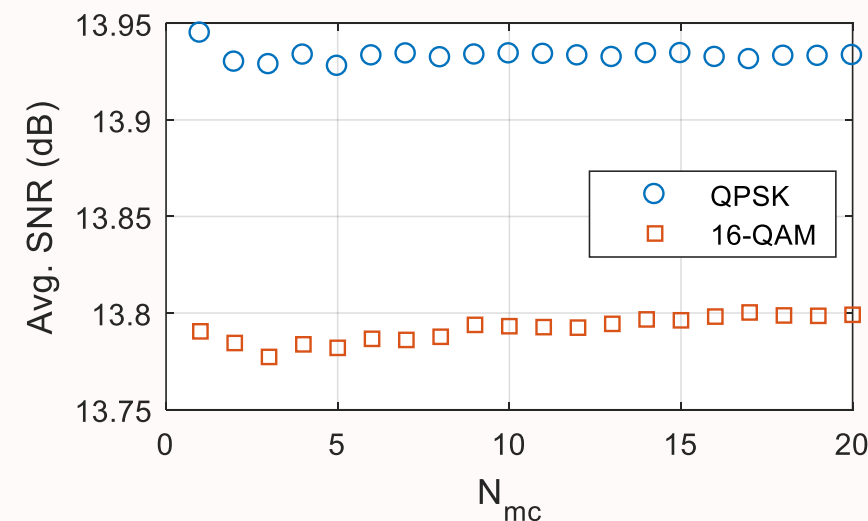
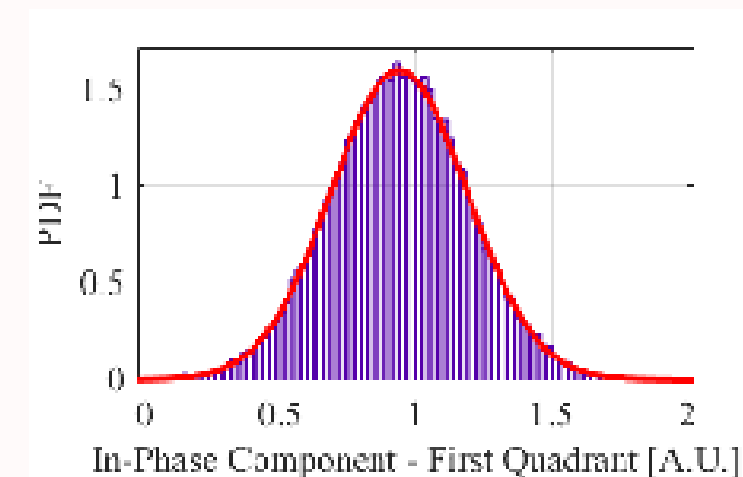
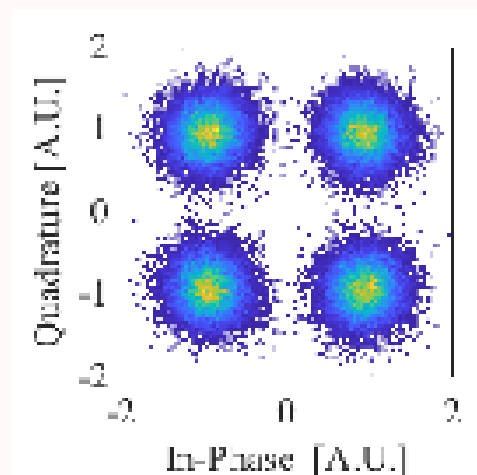
## ▪ Simulations

- FF.SS. solving the **ME**
- FF.SS. solving the **CNLSE** with random birefringence

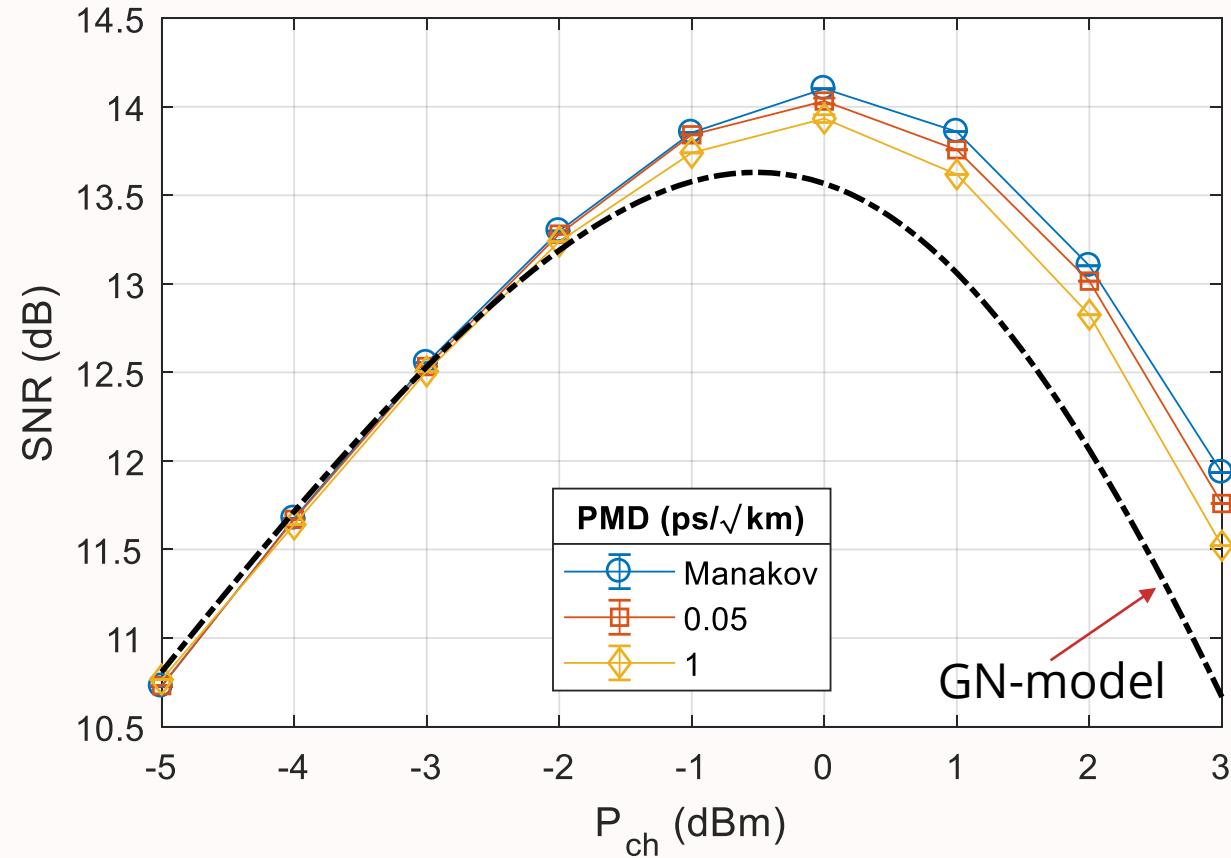
- **PMD =  $0.05 \text{ ps}/\sqrt{\text{km}}$  and  $1 \text{ ps}/\sqrt{\text{km}}$**
- Monte Carlo analyses on **20 different realizations**

# THE OBSERVED INTERFERENCE

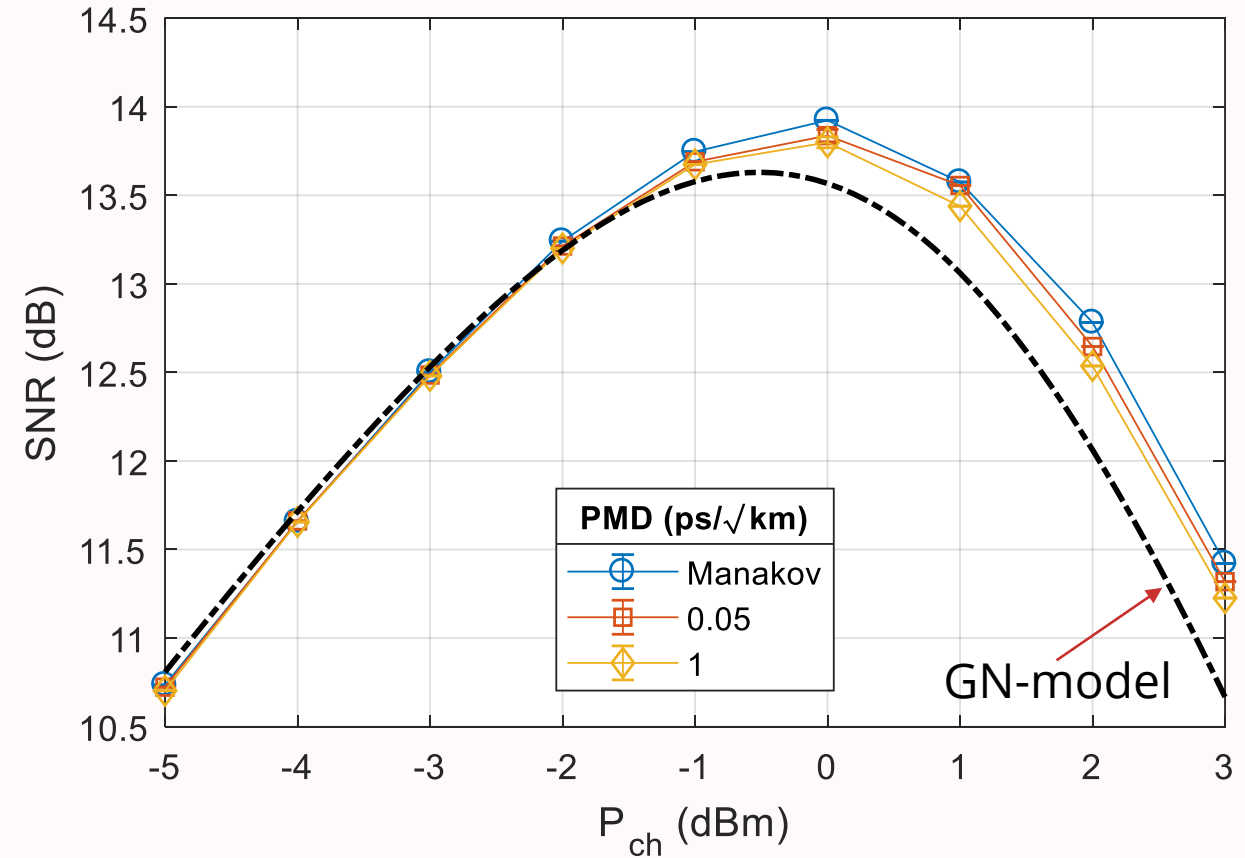
- **No** relevant **phase noise**
- **Gaussian**-distributed disturbance
- **20** Monte Carlo **runs** on PMD are sufficient to obtain a **good estimation**



## PM-QPSK



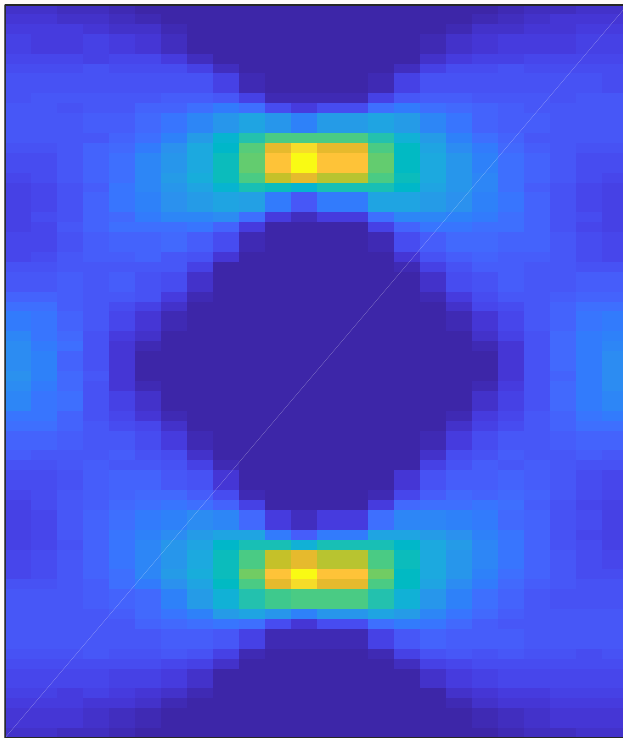
## PM-16QAM



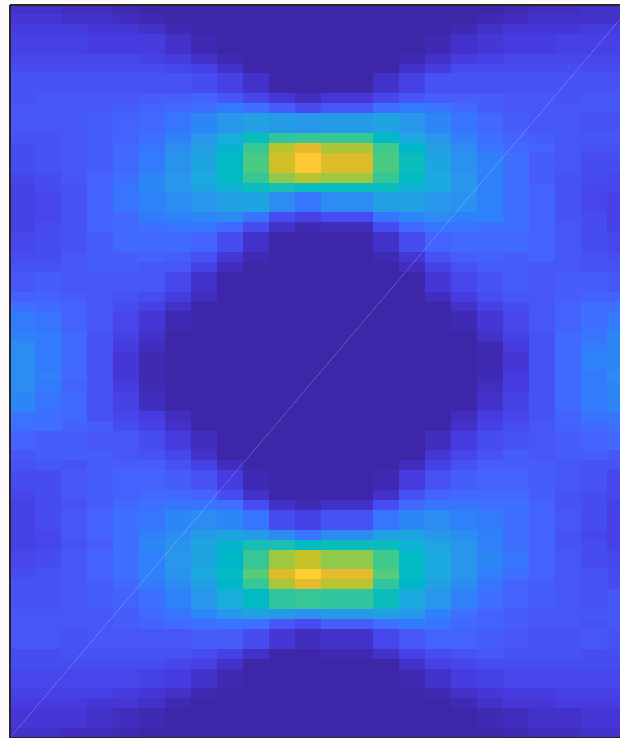
# PMD EFFECT ON SIGNAL GAUSSIAN-IZATION

Eye diagrams after PM-QPSK propagation over  $L_{\text{eff}}$ , SSMF, 20000 symbols average window

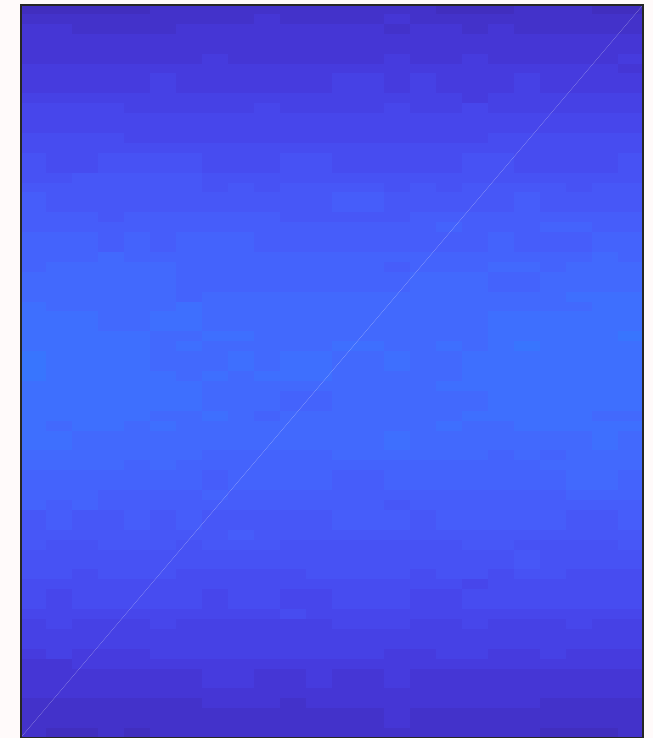
**Ideal**



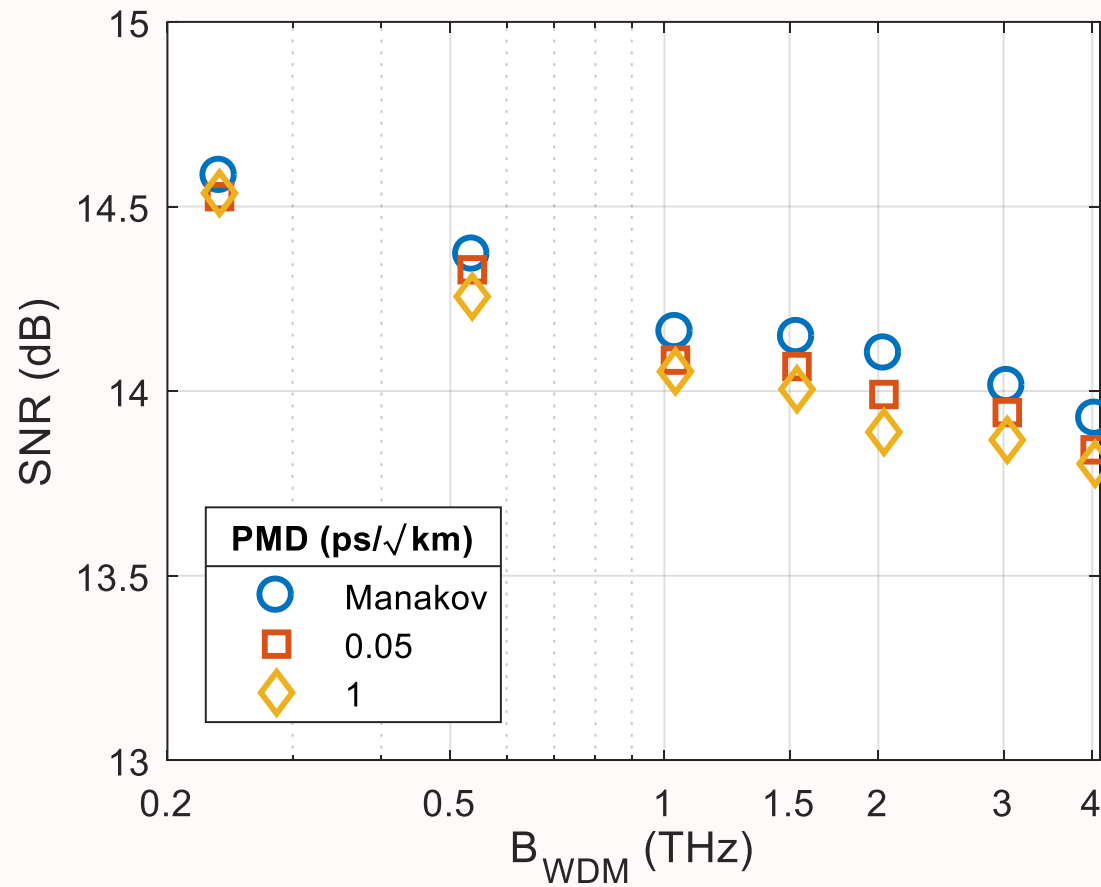
**PMD only**



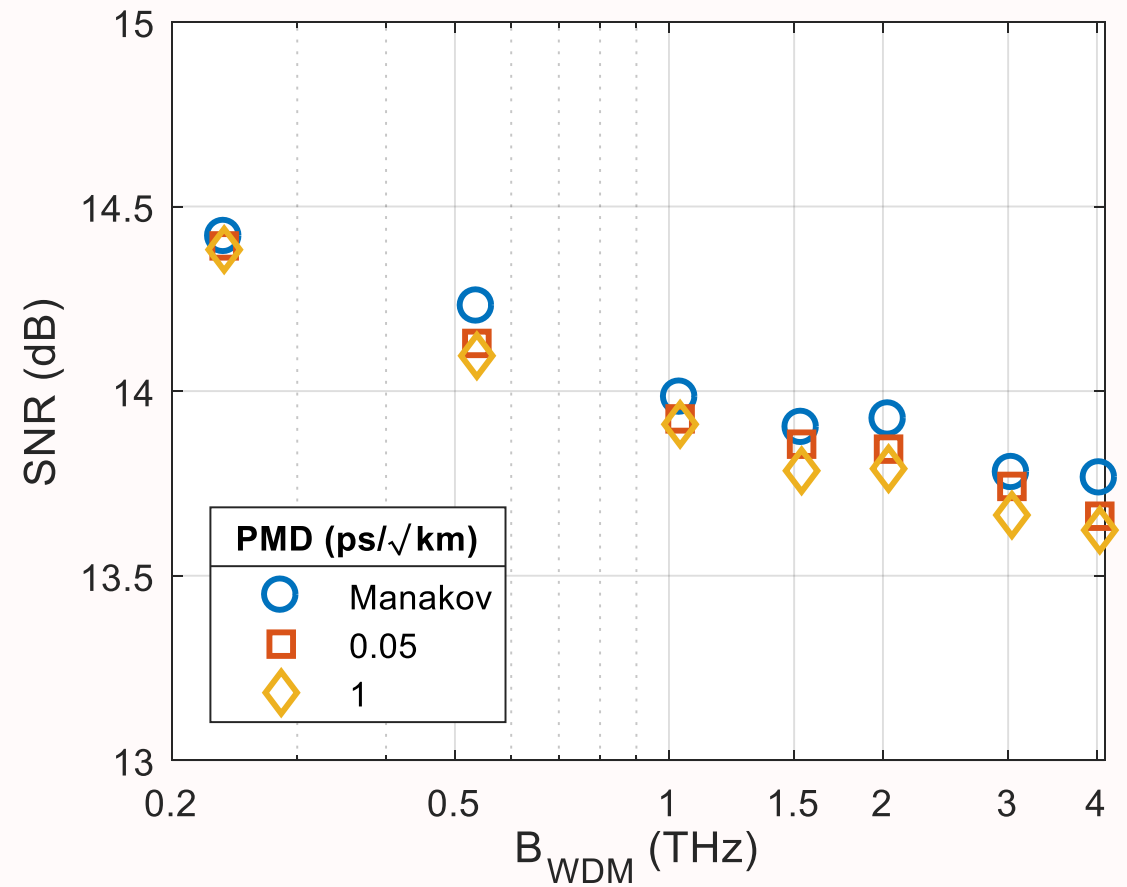
**CD+PMD**



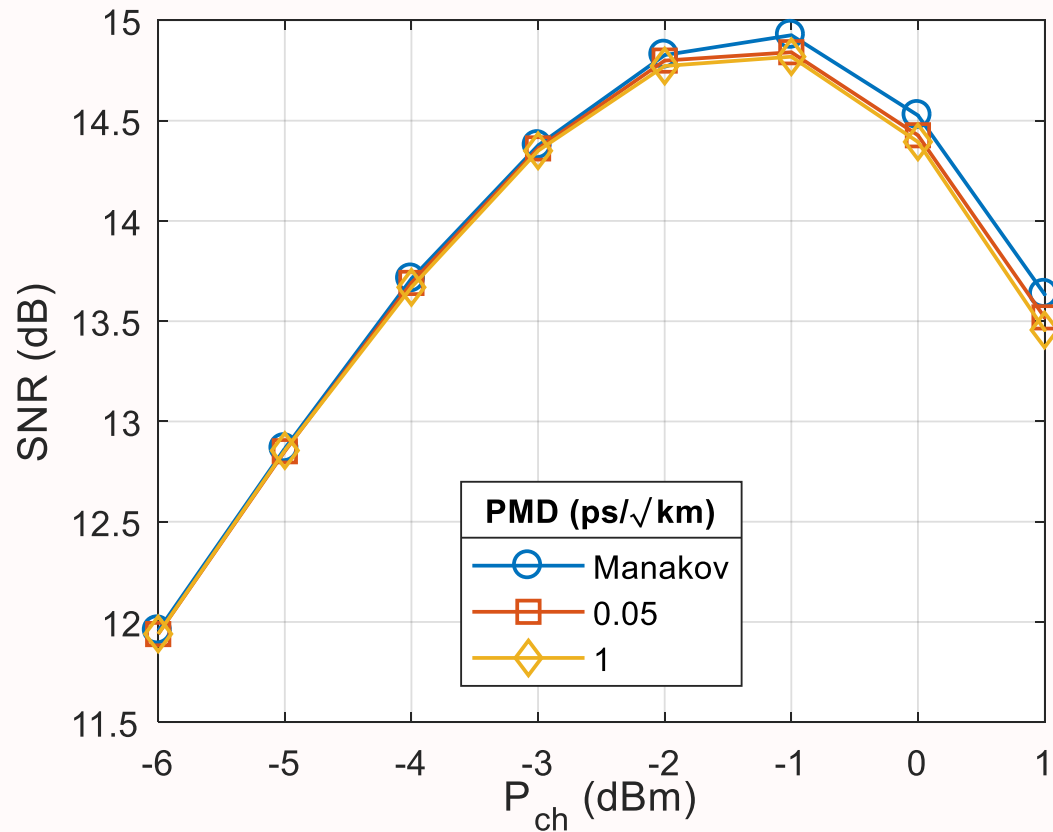
## PM-QPSK



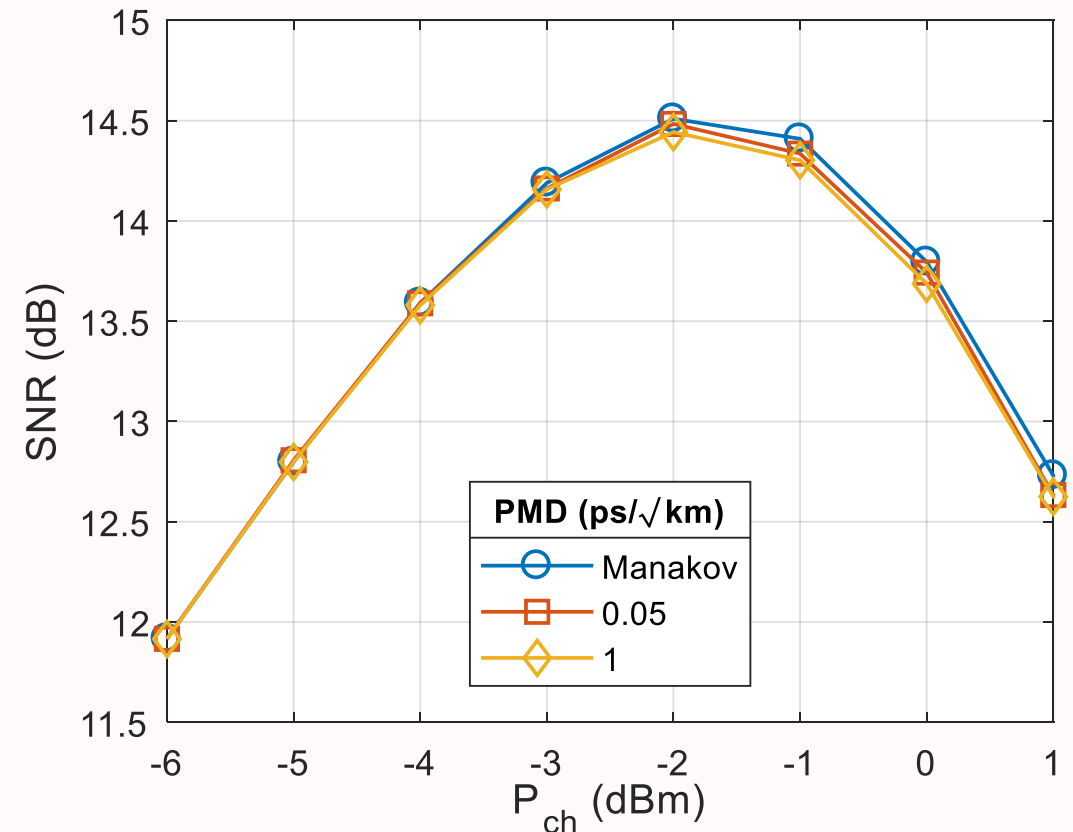
## PM-16QAM



## PM-QPSK



## PM-16QAM



- When propagating multilevel modulation formats **dominant impairment is ASE+NLI**, also **when considering random birefringence** and far exceeding the fiber coherence bandwidth
- **Statistical variations** with respect different realizations of random birefringence are **practically negligible**
- Results obtained integrating **ME and CNLSE+WM** are practically **superimposed**
- The only **effect of PMD is a minor speeding-up in Gaussian-ization** of signals: no relevant effect
- **ME can be used** to study propagation of multilevel modulation formats also **far beyond the theoretical validity bandwidth for ME** itself
- Consequently, **models derived** from the ME hold also at **large bandwidth**
- Gain/loss variations with space/frequency must be included, starting from the **interaction NLI-SRS: GGN\***
- **Presentation will be available at [www.optcom.polito.it/talks](http://www.optcom.polito.it/talks)**